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Bridging the Gap Between Underspecification Formalisms: Minimal Recursion Semantics as Dominance Constraints

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Abstract

Minimal Recursion Semantics (MRS) is the standard formalism used in large-scale HPSG grammars to model underspecified semantics. We present the first provably efficient algorithm to enumerate the readings of MRS structures, by translation into normal dominance constraints.

1 Introduction

In the past few years there has been considerable activity in the development of formalisms for *underspecified semantics* (Alshawi and Crouch, 1992; Reyle, 1993; Bos, 1996; Copestake et al., 1999; Egg et al., 2001). The common idea is to delay the enumeration of all readings for as long as possible. Instead, they work with a compact *underspecified representation* for as long as possible, only enumerating readings from this representation by need.

Minimal Recursion Semantics (MRS) (Copestake et al., 1999) is the standard formalism for semantic underspecification used in large-scale HPSG grammars (Pollard and Sag, 1994; Copestake and Flickinger, 2000). Despite of this clear relevance, the most obvious questions about MRS are still open:

1. Is it possible to enumerate the readings of MRS structures efficiently? No algorithm has been published so far. Existing implementations seem to be practical, even though the problem whether an MRS has a reading is NP-complete (Althaus et al., 2003, Theorem 10.1).
2. What is the precise relationship to other underspecification formalism? Are all of them the same, or else, what are the differences?

We distinguish the sublanguages of *MRS nets* and *normal dominance nets*, and show that they can be intertranslated. This translation answers the first question: existing constraint solvers for normal dominance constraints can be used to enumerate the readings of MRS nets in low polynomial time.

The translation also answers the second question, at least when restricted to pure scope underspecification. It shows the equivalence of a large fragment of MRSs and a corresponding fragment of normal dominance constraints, which in turn is equivalent to a large fragment of Hole Semantics (Bos, 1996) as proven in (Koller et al., 2003). Additional underspecified treatments of ellipsis or reinterpretation, however, are available for extensions of dominance constraint only (CLLS, the constraint language for lambda structures (Egg et al., 2001)).

Our results are subject to a new proof technique which reduces reasoning about MRS structures to reasoning about *weakly* normal dominance constraints (Bodirsky et al., 2003). The previous proof techniques for normal dominance constraints from (Koller et al., 2003) don't apply.

2 Minimal Recursion Semantics

We define a simplified version of Minimal Recursion Semantics and discuss differences to the original definitions in (Copestake et al., 1999).

MRS is a description language for formulas of some first order object languages with generalized quantifiers. Underspecified representations in MRS consist of *elementary predications* and *handle constraints*. Roughly, elementary predications are object language formulas with “holes” into which other formulas can be plugged; handle constraints restrict

the way these formulas can be plugged into each other. More formally, MRSs are formulas over the following vocabulary:

1. *Variables*. An infinite set of variables ranged over by h . Variables are also called *handles*.
2. *Constants*. An infinite set of constants ranged over by x, y, z . Constants are the *individual variables* of the object language.
3. *Function symbols*.
 - (a) A set of function symbols written as P .
 - (b) A set of quantifier symbols ranged over by Q (such as *every* and *some*). Pairs Q_x are further function symbols (the *variable binders* of x in the object language).
4. The symbol \leq for the outscopes relation.

Formulas of MRS have three kinds of literals, the first two are called *elementary predications* (EPs) and the third *handle constraints*:

1. $h:P(x_1, \dots, x_n, h_1, \dots, h_m)$ where $n, m \geq 0$
2. $h:Q_x(h_1, h_2)$
3. $h_1 \leq h_2$

Label positions are on the left of colons ‘:’ and *argument positions* on the right. Let M be a set of literals. The *label set* $\text{lab}(M)$ contains those handles of M that occur in label but not in argument position. The *argument handle set* $\text{arg}(M)$ contains the handles of M that occur in argument but not in label position.

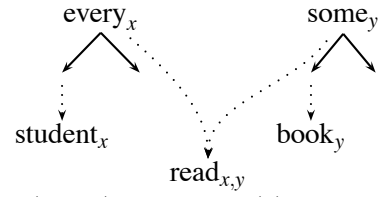
Definition 1 (MRS). An MRS is finite set M of MRS-literals such that:

- M1** Every handle occurs at most once in label and at most once in argument position in M .
- M2** Handle constraint $h_1 \leq h_2$ in M always relate argument handles h_1 to labels h_2 of M .
- M3** For every constant (individual variable) x in argument position in M there is a unique literal of the form $h:Q_x(h_1, h_2)$ in M .

We call an MRS *compact* if it additionally satisfies:

- M4** Every handle of M occurs exactly once in an elementary predication of M .

We say that a handle h *immediately outscopes* a handle h' in an MRS M iff there is an EP E in M such that h occurs in label and h' in argument position of E . The *outscopes relation* is the reflexive, transitive closure of the immediate outscopes relation.



$\{h_1 : \text{every}_x(h_2, h_4), h_3 : \text{student}(x), h_5 : \text{some}_y(h_6, h_8), h_7 : \text{book}(y), h_9 : \text{read}(x, y), h_2 \leq h_3, h_6 \leq h_7\}$

Figure 1: MRS for “Every student reads a book”.

An example MRS for the scopally ambiguous sentence “Every student reads a book” is given in Fig. 1. We often represent MRSs by directed graphs whose nodes are the handles of the MRS. Elementary predications are represented by solid edges and handle constraints by dotted lines. Note that we make the relation between bound variables and their binders explicit by dotted lines (as from every_x to $\text{read}_{x,y}$); redundant “binding-edges” that are subsumed by sequences of other edges are omitted however (from every_x to student_x for instance).

A solution for an underspecified MRS is called a *configuration*, or *scope-resolved MRS*.

Definition 2 (Configuration). An MRS M is a *configuration* if it satisfies the following conditions.

- C1** The graph of M is a tree of solid edges: handles don’t properly outscopes themselves or occur in different argument positions and all handles are pairwise connected by elementary predications.
- C2** If two EPs $h:P(\dots, x, \dots)$ and $h_0:Q_x(h_1, h_2)$ belong to M , then h_0 outscopes h in M (so that the binding edge from h_0 to h is redundant).

We call M a *configuration for* another MRS M' if there exists some substitution $\sigma : \text{arg}(M') \mapsto \text{lab}(M')$ which states how to identify argument handles of M' with labels of M' , so that:

- C3** $M = \{\sigma(E) \mid E \text{ is EP in } M'\}$, and
- C4** $\sigma(h_1)$ outscopes h_2 in M , for all $h_1 \leq h_2 \in M'$.

The value $\sigma(E)$ is obtained by substituting all argument handles in E , leaving all others unchanged.

The MRS in Fig. 1 has precisely two configurations displayed in Fig. 2 which correspond to the two readings of the sentence. In this paper, we present an algorithm for scope underspecification that can enumerate the configurations of MRSs on need.

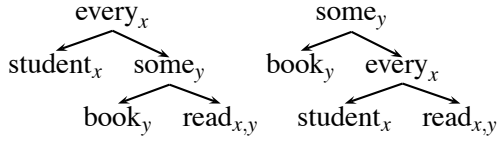


Figure 2: Graphs of Configurations.

Differences to Standard MRS. Our version departs from standard MRS in some respects. First, we assume that different EPs must be labeled with different handles, and that labels cannot be identified. In standard MRS, however, conjunctions are encoded by labeling different EPs with the same handle. These EP-conjunctions can be replaced in a preprocessing step introducing additional EPs that make conjunctions explicit.

Second, our outscope constraints are slightly less restrictive than the original “qeq-constraints.” A handle h is qeq to a handle h' in an MRS M , $h =_q h'$, if either $h = h'$ or a quantifier $h: Q_x(h_1, h_2)$ occurs in M and h_2 is qeq to h' in M . Thus, $h =_q h'$ implies $h \leq h'$, but not the other way round. We believe that the additional strength of qeq-constraints is not needed in practice for modeling scope. Recent work in semantic construction for HPSG (Copestake et al., 2001) supports our conjecture: the examples discussed there are compatible with our simplification.

Third, we depart in some minor details: we use sets instead of multi-sets and omit top-handles which are useful only during semantics construction.

3 Dominance Constraints

Dominance constraints are a general framework for describing trees, and thus syntax trees of logic formulas. Dominance constraints are the core language underlying CLLS (Egg et al., 2001) which adds parallelism and binding constraints.

3.1 Syntax and Semantics

We assume a possibly infinite signature Σ of function symbols with fixed arities and an infinite set Var of variables ranged over by X, Y, Z . We write f, g for function symbols and $\text{ar}(f)$ for the arity of f .

A dominance constraint φ is a conjunction of dominance, inequality, and labeling literals of the following forms where $\text{ar}(f) = n$:

$$\varphi ::= X \triangleleft^* Y \mid X \neq Y \mid X : f(X_1, \dots, X_n) \mid \varphi \wedge \varphi'$$

Dominance constraints are interpreted over finite constructor trees, i.e. ground terms constructed from the function symbols in Σ . We identify ground terms with trees that are rooted, ranked, edge-ordered and labeled. A solution for a dominance constraint consists of a tree τ and a variable assignment α that maps variables to nodes of τ such that all constraints are satisfied: a labeling literal $X : f(X_1, \dots, X_n)$ is satisfied iff the node $\alpha(X)$ is labeled with f and has daughters $\alpha(X_1), \dots, \alpha(X_n)$ in this order; a dominance literal $X \triangleleft^* Y$ is satisfied iff $\alpha(X)$ is an ancestor of $\alpha(Y)$ in τ ; and an inequality literal $X \neq Y$ is satisfied iff $\alpha(X)$ and $\alpha(Y)$ are distinct nodes.

Note that solutions may contain additional material. The tree $f(a, b)$, for instance, satisfies the constraint $Y : a \wedge Z : b$.

3.2 Normality and Weak Normality

The satisfiability problem of arbitrary dominance constraints is NP-complete (Koller et al., 2001) in general. However, Althaus et al. (2003) identify a natural fragment of so called *normal dominance constraints*, which have a polynomial time satisfiability problem. Bodirsky et al. (2003) generalize this notion to *weakly normal dominance constraints*.

We call a variable a *hole* of φ if it occurs as in argument position in φ and a *root* of φ otherwise.

Definition 3. A dominance constraint φ is *normal* (and compact) if it satisfies the following conditions.

- N1** (a) each variable of φ occurs at most once in the labeling literals of φ .
(b) each variable of φ occurs at least once in the labeling literals of φ .
- N2** for distinct roots X and Y of φ , $X \neq Y$ is in φ .
- N3** (a) if $X \triangleleft^* Y$ occurs in φ , Y is a root in φ .
(b) if $X \triangleleft^* Y$ occurs in φ , X is a hole in φ .

A dominance constraint is *weakly normal* if it satisfies all above properties except for **N1**(b) and **N3**(b).

The idea behind (weak) normality is that the constraint graph (see below) of a dominance constraint consists of solid fragments which are connected by dominance constraints; these fragments may not properly overlap in solutions.

Note that Definition 3 always imposes compactness, meaning that the height of solid fragments is at most one. This is not a serious restriction, as for MRS, since more general weakly normal dominance

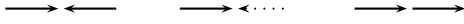
constraints can be compactified, provided that dominance links relate either roots or holes with roots.

Dominance Graphs. We often represent dominance constraints as *graphs*. A *dominance graph* is the directed graph $(V, \triangleleft^* \uplus \triangleleft)$. The graph of a weakly normal constraint φ is defined as follows: The nodes of the graph of φ are the variables of φ . A labeling literal $X : f(X_1, \dots, X_n)$ of φ contributes *tree edges* $(X, X_i) \in \triangleleft$ for $1 \leq i \leq n$ that we draw as $X \rightarrow X_i$; we freely omit the label f and the edge order in the graph. A dominance literal $X \triangleleft^* Y$ contributes a dominance edge $(X, Y) \in \triangleleft^*$ that we draw as $X \cdots \rightarrow Y$. Inequality literals in φ are also omitted in the graph.

For example, the constraint graph on the right represents the dominance constraint $X : f(X') \wedge Y : g(Y') \wedge X' \triangleleft^* Z \wedge Y' \triangleleft^* Z \wedge Z : a \wedge X \neq Y \wedge X \neq Z \wedge Y \neq Z$



A dominance graph is *weakly normal* or a *wnd-graph* if it does not contain any forbidden subgraphs:



Dominance graphs of a weakly normal dominance constraints are obviously weakly normal.

Solved Forms and Configurations. The main difference between MRS and dominance constraints lies in their notion of interpretation: solutions versus configurations.

Every satisfiable dominance constraint has infinitely many solutions. Algorithms for dominance constraints therefore do not enumerate solutions but *solved forms*. We say that a dominance constraint is in solved form iff its graph is in solved form. A wnd-graph Φ is in solved form iff Φ is a forest. The *solved forms of Φ* are solved forms Φ' that are more specific than Φ , i.e. Φ and Φ' differ only in their dominance edges and the reachability relation of Φ extends the reachability of Φ' . A *minimal solved form of Φ* is a solved form of Φ that is minimal with respect to specificity.

The notion of configurations from MRS applies to dominance constraints as well. Here, a *configuration* is a dominance constraint whose graph is a tree without dominance edges. A configuration of a constraint φ is a configuration that solves φ in the obvious sense. *Simple solved forms* are tree-shaped solved forms where every hole has exactly one outgoing dominance edge.

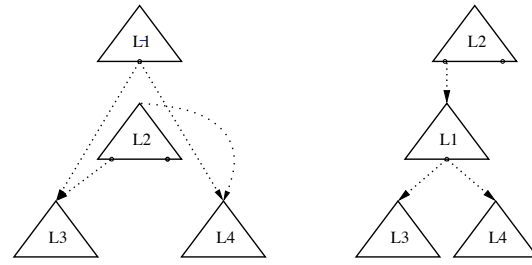


Figure 3: A dominance constraint (left) with a minimal solved form (right) that has no configuration.

Lemma 1. Simple solved forms and configurations correspond: Every simple solved form has exactly one configuration, and for every configuration there is exactly one solved form that it configures.

Unfortunately, Lemma 1 does not extend to minimal instead of simple solved forms: there are minimal solved forms without configurations. The constraint on the right of Fig. 3, for instance, has no configuration: the hole of L1 would have to be filled twice while the right hole of L2 cannot be filled.

4 Representing MRSs

We next map MRSs to weakly normal dominance constraints so that configurations are preserved. Unfortunately, this translation is based on a non-standard semantics for dominance constraints, namely configurations. We address this problem in the following sections.

The translation of an MRS M to a dominance constraint φ_M is quite trivial. The variables of φ_M are the handles of M and its literal set is:

$$\begin{aligned} & \{h : P_{x_1, \dots, x_n}(h_1, \dots) \mid h : P(x_1, \dots, x_n, h_1, \dots) \in M\} \\ & \cup \{h : Q_x(h_1, h_2) \mid h : Q_x(h_1, h_2) \in M\} \\ & \cup \{h_1 \triangleleft^* h_2 \mid h_1 \leq h_2 \in M\} \\ & \cup \{h \triangleleft^* h_0 \mid h : Q_x(h_1, h_2), h_0 : P(\dots, x, \dots) \in M\} \\ & \cup \{h \neq h' \mid h, h' \text{ in distinct label positions of } M\} \end{aligned}$$

Compact MRSs M are clearly translated into (compact) weakly normal dominance constraints. Labels of M become roots in φ_M while argument handles become holes. Weak root-to-root dominance literals are needed to encode MRS's variable binding condition C2. It could be formulated equivalently through lambda binding constraints of CLLS (but this is not necessary here in the absence of parallelism).

Proposition 1. The translation of a compact MRS M into a weakly normal dominance constraint φ_M preserves configurations.

This weak correctness property follows straightforwardly from the analogy in the definitions.

5 Constraint Solving

We recall an algorithm from (Bodirsky et al., 2003) that efficiently enumerates all minimal solved forms of wnd-graphs or constraints. All results of this section are proved there.

The algorithm can be used to enumerate configurations for a large subclass of MRSs, as we will see in Section 6. But equally importantly, this algorithm provides a powerful proof method for reasoning about solved forms and configurations on which all our results rely.

5.1 Weak Connectedness

Two nodes X and Y of a wnd-graph $\Phi = (V, E)$ are *weakly connected* if there is an undirected path from X to Y in (V, E) . We call Φ weakly connected if all its nodes are weakly connected. A weakly connected component (wcc) of Φ is a maximal weakly connected subgraph of Φ . The wccs of $\Phi = (V, E)$ form proper partitions of V and E .

Proposition 2. The graph of a solved form of a weakly connected wnd-graph is a tree.

5.2 Freeness

The idea of the enumeration algorithm is based on the notion of *freeness*.

Definition 4. A node X of a wnd-graph Φ is called *free* in Φ if there exists a solved form of Φ whose graph is a tree with root X .

A weakly connected wnd-graph without free nodes is unsolvable. Otherwise, it has a solved form whose graph is a tree (Prop. 2) and the root of this tree is free in Φ .

Given a set of nodes $V' \subseteq V$, we write $\Phi|_{V'}$ for the restriction of Φ to nodes in V' and edges in $V' \times V'$. The following lemma characterizes freeness:

Lemma 2. A wnd-graph Φ with free node X satisfies the freeness conditions:

F1 node X has indegree zero in graph Φ , and

F2 no distinct children Y and Y' of X in Φ that are linked to X by immediate dominance edges are weakly connected in the remainder $\Phi|_{V \setminus \{X\}}$.

5.3 Algorithm

The algorithm for enumerating the minimal solved forms of a wnd-graph (or equivalently constraint) is given in Fig. 4. We illustrate the algorithm for the problematic wnd-graph Φ in Fig. 3. The graph of Φ is weakly connected, so that we can call $\text{solve}(\Phi)$. This procedure guesses topmost fragments in solved forms of Φ (which always exist by Prop. 2).

The only candidates are L1 or L2 since L3 and L4 have incoming dominance edges which violates F1. Let us choose the fragment L2 to be topmost. The graph which remains when removing L2 is still weakly connected. It has a single minimal solved form computed by a recursive call of the solver, where L1 dominates L3 and L4. The solved form of the restricted graph is then put below the left hole of L2, since it is connected to this hole. As a result, we obtain the solved form on the right of Fig. 3.

Theorem 1. The function $\text{solved-form}(\Phi)$ computes all minimal solved forms of a weakly normal dominance graph Φ ; it runs in quadratic time per solved form.

6 Full Translation

We next explain how to encode a large class of MRSs into wnd-constraints such that configurations correspond precisely to minimal solved forms. The result of the translation will indeed be normal.

6.1 Problems and Examples

The naive representation of MRSs as weakly normal dominance constraints is only correct in a weak sense. The encoding fails in that some MRSs which have no configurations are mapped to solvable wnd-constraints. For instance, this holds for the MRS on the right in Fig 3.

We cannot even hope to translate arbitrary MRSs correctly into wnd-constraints: the configurability problem of MRSs is NP-complete, while satisfiability of wnd-constraints can be solved in polynomial time. Instead, we introduce the sublanguages of *MRS-nets* and equivalent *wnd-nets*, and show that they can be intertranslated in quadratic time.

$\text{solved-form}(\Phi) \equiv$
 Let Φ_1, \dots, Φ_k be the wccs of $\Phi = (V, E)$
 Let (V_i, E_i) be the result of $\text{solve}(\Phi_i)$
return $(V, \cup_{i=1}^k E_i)$
 $\text{solve}(\Phi) \equiv$
precond: $\Phi = (V, \triangleleft \sqcup \triangleleft^*)$ is weakly connected
choose a node X satisfying (F1) and (F2) in Φ **else fail**
 Let Y_1, \dots, Y_n be all nodes s.t. $X \triangleleft Y_i$
 Let Φ_1, \dots, Φ_k be the weakly connected components of $\Phi|_{V - \{X, Y_1, \dots, Y_n\}}$
 Let (W_j, E_j) be the result of $\text{solve}(\Phi_j)$, and $X_j \in W_j$ its root
return $(V, \cup_{j=1}^k E_j \cup \triangleleft \cup \triangleleft_1^* \cup \triangleleft_2^*)$ where
 $\triangleleft_1^* = \{(Y_i, X_j) \mid \exists X' : (Y_i, X') \in \triangleleft^* \wedge X' \in W_j\}$,
 $\triangleleft_2^* = \{(X, X_j) \mid \neg \exists X' : (Y_i, X') \in \triangleleft^* \wedge X' \in W_j\}$

Figure 4: Enumerating the minimal solved-forms of a wnd-graph.

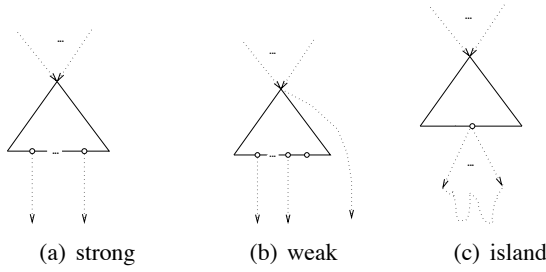


Figure 5: Fragment Schemas of Nets

6.2 Dominance and MRS-Nets

A hypernormal path (Althaus et al., 2003) in a wnd-graph is a sequence of adjacent edges that does not traverse two outgoing dominance edges of some hole X in sequence, i.e. a wnd-graph without situations $Y_1 \triangleleft \dots \triangleleft X \triangleleft \dots \triangleleft Y_2$.

A dominance net φ is a weakly normal dominance constraint whose fragments all satisfy one of the three schemas in Fig. 5. MRS-nets can be defined analogously. This means that all roots of φ are labeled in φ , and that all fragments $X : f(X_1, \dots, X_n)$ of φ satisfy one of the following three conditions:

strong. $n \geq 0$ and for all $Y \in \{X_1, \dots, X_n\}$ there exists a unique Z such that $Y \triangleleft^* Z$ in φ , and there exists no Z such that $X \triangleleft^* Z$ in φ .

weak. $n \geq 1$ and for all $Y \in \{X_1, \dots, X_{n-1}, X\}$ there exists a unique Z such that $Y \triangleleft^* Z$ in φ , and there exists no Z such that $X_n \triangleleft^* Z$ in φ .

island. $n = 1$ and all variables in $\{Y \mid X_1 \triangleleft^* Y \text{ in } \varphi\}$ are connected by a hypernormal path in the graph of

the restricted constraint $\varphi|_{V - \{X_1\}}$, and there exists no weak dominance edge $X \triangleleft^* Z$ for any Z in φ .

The requirement of hypernormal connections in islands replaces the notion of chain-connectedness in (Koller et al., 2003), which fails to apply to dominance constraints with weak dominance edges.

For expository ease, we restrict ourselves to a simple version of island-fragments. In general, we could allow for islands with $n > 1$.

6.3 Normalizing Dominance Nets

Dominance nets are wnd-constraints. We next translate dominance nets φ to normal dominance constraints φ' such φ has a configuration iff φ' is satisfiable. The trick is to normalize weak dominance edges. The normalization $\text{norm}(\varphi)$ of a weakly normal dominance constraint φ is obtained by converting all root-to-root dominance literals $X \triangleleft^* Y$ as follows:

$$X \triangleleft^* Y \Rightarrow X_n \triangleleft^* Y$$

if X roots a fragment of φ that satisfies schema weak of net fragments. If φ is a dominance net then $\text{norm}(\varphi)$ is indeed a normal dominance net.

Theorem 2. The configurations of a weakly connected dominance net φ correspond bijectively to the minimal solved forms of its normalization $\text{norm}(\varphi)$.

For illustration, consider the problematic wnd-constraint φ on the left of Fig. 3. φ has two minimal solved forms with top-most fragments L1 and L2 re-

spectively. The former can be configured, in contrast to the later which is drawn on the right of Fig. 3.

Normalizing φ has an interesting consequence: $\text{norm}(\varphi)$ has (in contrast to φ) a single minimal solved form with L1 on top. Indeed, $\text{norm}(\varphi)$ can not be satisfied while placing L2 topmost. Our algorithm detects this correctly: the normalization of fragment L2 is not free in $\text{norm}(\varphi)$ since it violates property F2.

The proof of Theorem 2 captures the rest of this section. We will show in a first step (Prop. 3) that the configurations are preserved when normalizing weakly connected and satisfiable nets. In the second step, we show that minimal solved forms of normalized nets, and thus of $\text{norm}(\varphi)$, can always be configured (Prop. 4).

Corollary 1. Configurability of weakly connected MRS-nets can be decided in polynomial time; configurations of weakly connected MRS-nets can be enumerated in quadratic time per configuration.

6.4 Correctness Proof

Most importantly, nets can be recursively decomposed into nets as long as they have configurations:

Lemma 3. If a dominance net φ has a configuration whose top-most fragment is $X : f(X_1, \dots, X_n)$, then the restriction $\varphi|_{V - \{X, X_1, \dots, X_n\}}$ is a dominance net.

Note that the restriction of the problematic net φ by L2 on the left in Fig. 3 is not a net. This does not contradict the lemma, as φ does not have a configuration with top-most fragment L2.

Proof. First note that as X is free in φ it cannot have incoming edges (condition F1). This means that the restriction deletes only dominance edges that depart from nodes in $\{X, X_1, \dots, X_n\}$. Other fragments thus only loose ingoing dominance edges by normality condition N3. Such deletions preserve the validity of the schemas *weak* and *strong*.

The island schema is more problematic. We have to show that the hypernormal connections in this schema can never be cut. So suppose that $Y : f(Y_1)$ is an island fragment with outgoing dominance edges $Y_1 \triangleleft^* Z_1$ and $Y_1 \triangleleft^* Z_2$, so that Z_1 and Z_2 are connected by some hypernormal path traversing the deleted fragment $X : f(X_1, \dots, X_n)$. We distinguish the three possible schemata of this fragment:

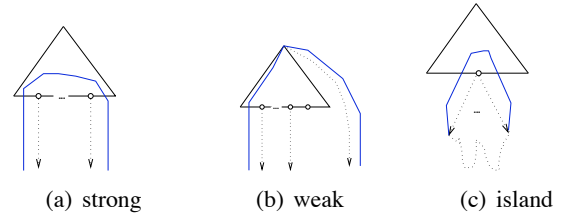


Figure 6: Traversals through fragments of free roots

strong: since X does not have incoming dominance edges, there is only a single non-trivial kind of traversals, drawn in Fig. 6(a). But such traversals contradict the freeness of X according to F2.

weak: there is one other way of traversing weak fragments, shown in Fig. 6(b). Let $X \triangleleft^* Y$ be the weak dominance edge. The traversal proves that Y belongs to the weakly connected components of one of the X_i , so the $\varphi \wedge X_n \triangleleft^* Y$ is unsatisfiable. This shows that the hole X_n cannot be identified with any root, i.e., φ does not have any configuration in contrast to our assumption.

island: free island fragments permit one single non-trivial form of traversals, depicted in Fig. 6(c). But such traversals are not hypernormal. \square

Proposition 3. A configuration of a weakly connected dominance net φ configures its normalization $\text{norm}(\varphi)$, and vice versa of course.

Proof. Let C be a configuration of φ . We show that it also configures $\text{norm}(\varphi)$. Let S be the simple solved form of φ that is configured by C (Lemma 1), and S' be a minimal solved form of φ which is more general than S .

Let $X : f(Y_1, \dots, Y_n)$ be the top-most fragment of the tree S . This fragment must also be the top-most fragment of S' , which is a tree since φ is assumed to be weakly connected (Prop. 2). S' is constructed by our algorithm (Theorem 1), so that the evaluation of $\text{solve}(\varphi)$ must choose X as free root in φ .

Since φ is a net, some literal $X : f(Y_1, \dots, Y_n)$ must belong to φ . Let $\varphi' = \varphi|_{\{X, Y_1, \dots, Y_n\}}$ be the restriction of φ to the lower fragments. The weakly connected components of all Y_1, \dots, Y_{n-1} must be pairwise disjoint by F2 (which holds by Lemma 2 since X is free in φ). The X -fragment of net φ must satisfy one of three possible schemata of net fragments:

weak fragments: there exists a unique weak dominance edge $X \triangleleft^* Z$ in φ and unique hole Y_n without

outgoing dominance edge. The variable Z must be a root in φ and thus labeled. If Z is equal to X then φ were unsatisfiable by normality condition N2, which is impossible. Hence, Z occurs in the restriction φ' but not in the weakly connected components of any Y_1, \dots, Y_{n-1} . Otherwise, the minimal solved form S' could not be configured since the hole Y_n could not be identified with any root. Furthermore, the root of the Z -component must be identified with Y_n in any configuration of φ with root X . Hence, C satisfies $Y_n \triangleleft^* Z$ add by normalization.

The restriction φ' must be a dominance net by Lemma 3, and hence, all its weakly connected components are nets. For all $1 \leq i \leq n-1$, the component of Y_i in φ' is configured by the subtree of C at node Y_i , while the subtree of C at node Y_n configures the component of Z in φ' . The induction hypothesis yields that the normalizations of all these components are configured by the respective subconfigurations of C . Hence, $\text{norm}(\varphi)$ is configured by C .

strong or inland fragments are not altered by normalization, so that we can recurse to the lower fragments (if there exist any). \square

Proposition 4. Minimal solved forms of normal, weakly connected dominance nets have configurations.

Proof. By induction over the construction of minimal solved forms, we can show that all holes of minimal solved forms have a unique outgoing dominance edge at each hole. Furthermore, all minimal solved forms are trees since we assumed connectedness (Prop.2). Thus, all minimal solved forms are simple, so they have configurations (Lemma 1). \square

7 Conclusion

We have related two underspecification formalism, MRS and normal dominance constraints. We have distinguished the sublanguages of MRS-nets and normal dominance nets that are sufficient to model scope underspecification, and proved their equivalence. Thereby, we have obtained the first provably efficient algorithm to enumerate the readings of underspecified semantic representations in MRS.

Finally, our encoding has the advantage that researchers interested in dominance constraints can soon benefit from the large grammar resources of

MRS. This requires further work in order to deal with unrestricted versions of MRS used in practice. Conversely, one can now lift the additional modeling power of CLLS to MRS.

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